

On the transcendental part of $K3$ surfaces associated with 3D Fano polytopes

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Up to affine transformations over \mathbf{Z} there are 18 different 3D Fano polytopes. The set of vertices of such a polytope is a subset \mathbf{V} of \mathbf{Z}^3 which can be used as exponents for a Laurent polynomial. The surface in \mathbf{P}^3 defined by the homogenization of such a Laurent polynomial is a quartic $K3$ surface. Varying the coefficients of the Laurent polynomial yields a family of $K3$ surfaces. The aim of the talk is to demonstrate how the Gelfand-Kapranov-Zelevinsky hypergeometric system associated with \mathbf{V} and results on Mirror Symmetry for lattice polarized $K3$ surfaces lead to simple elegant expressions for the transcendental periods as functions of the coefficients of the Laurent polynomial.